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# A NETWORK FOR COMPENSATING THE SPECTRUM OF THE 6D4 MINIATURE GAS TRIODE

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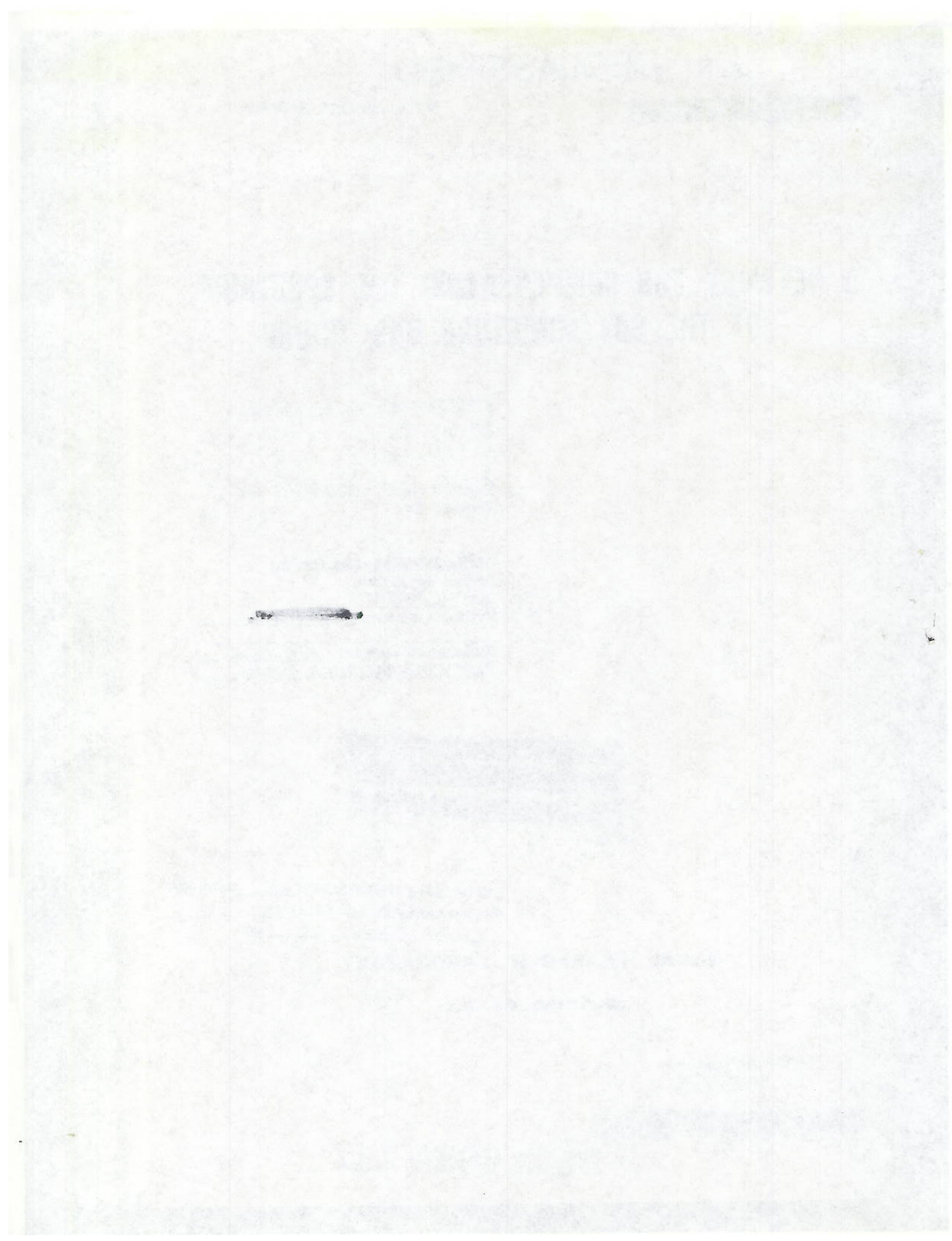
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# A NETWORK FOR COMPENSATING THE SPECTRUM OF THE 6D4 MINIATURE GAS TRIODE

G. C. Page, Jr.

June 29, 1949

Approved by:

H. O. Lorenzen, Head (Acting), Radio Countermeasures Branch  
L. A. Gebhard, Superintendent, Radio Division II



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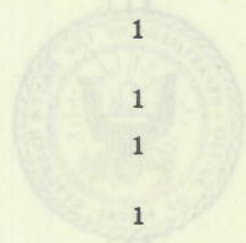
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ABSTRACT

A method has been developed for calculating a practical network to permit the use of the 6D4 miniature gas triode as a noise source in jamming transmitters. The compensating network flattens the spectrum of the 6D4 tube to within three decibels, and contains adjustable circuit elements to take care of variations between tubes. It has been used successfully over the frequency range of 50 kc to 5 Mc.

PROBLEM STATUS

This is an interim report; work on the problem is continuing.

AUTHORIZATION

NRL Problem R06-21R (S-1249X-C)

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## A NETWORK FOR COMPENSATING THE SPECTRUM OF THE 6D4 MINIATURE GAS TRIODE

### INTRODUCTION

The 6D4 miniature gas tube has been used with considerable success as a noise source in jamming transmitters. Because of the 30 to 40 db variation in the noise voltage output of this tube over the frequency range of 50 kc to 5 Mc, it was first thought that the modulator, into which the noise was injected, must be equalized. If, however, this noise spectrum could be flattened before it was fed into an amplifier or modulator, much of the trial and error compensation could be avoided, and a flat amplifier could be designed from the beginning.

This flattening was accomplished at the Laboratory by inserting a network<sup>1</sup> between the noise source and the first stage of amplification. Since many difficulties existed in precisely determining the internal impedance of the 6D4 noise generator, logical trial and error methods have heretofore been utilized to obtain an acceptable network. The network is now placed on a calculable basis, is adjustable to counteract differences in 6D4 tubes, and has been successfully used to compensate a number of these tubes.

### GENERAL PROBLEM ANALYSIS

The circuit in which the 6D4 is used as a noise generator is shown in Figure 1 and its equivalent network in Figure 2. In order to determine  $Z$  on Figure 2 theoretically, it is necessary to obtain the noise spectrum of the generator over the range of 50 kc to 5 Mc, with the aid of a tuned radio-frequency noise analyzer of low input-capacity and high input-resistance. In making the spectrum analysis,  $C_K$  (Figures 1 and 2) is purposely very large so that it presents a short circuit to the noise generator over the desired frequency range. A brief consideration of Figure 3, the equivalent circuit of the 6D4 when connected to the noise spectrum analyzer, shows that  $V$ , the internal voltage, is unknown; and that  $Z$ , which may be complex, is also unknown. If  $Z$  is complex, a solution is not possible because there are only two available equations and at least three unknown quantities. Loading the generator with a condenser to obtain another equation is futile because the tube then emits pulses of noise or reacts in a random fashion as a relaxation oscillator. A variable inductance placed in series with the noise generator creates spurious oscillations in the analyzer because of magnetic coupling between the coils in the analyzer and the external inductance.

<sup>1</sup>Miles, J. M., "Experimental Jamming Transmitter Using a 200 Watt CWX-Band Developmental Magnetron," NRL Report No. R-3384 (Confidential), pp 5 and 7, 17 November 1948

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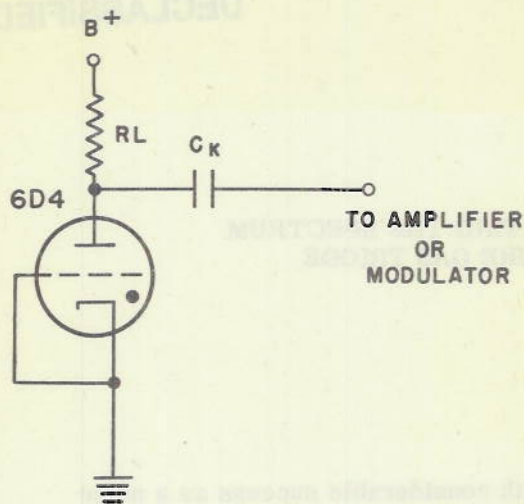


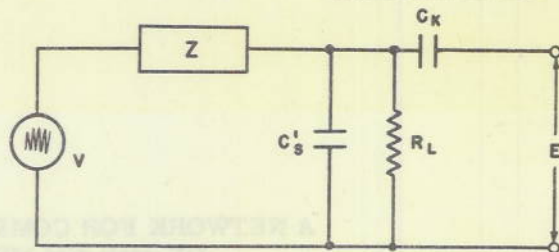
Figure 1 - Circuit for 6D4 as noise generator

It was hoped at first that either the capacitor or the inductor could be resonated with the internal impedance of the generator on the premise that  $Z$  was a varying series-resonant circuit; that is, that the  $R$ ,  $L$ , and  $C$  of  $Z$  varied with frequency but had resonant points detectable at several frequencies. Since the two externally connected parameters introduced unusable oscillatory phenomena, resistive loading was tried with the simplifying assumption that the internal impedance was not complex, but was a pure resistance.

Because  $C'_S$  and  $C_i$  have negligible effect on the circuit of Figure 3 at the low-frequency end of the noise spectrum, they are omitted from the calculations which follow.  $C_K$ ,  $R_i$ , and  $R_L$  are also omitted from computations, for, they too have a trivial consequence on the circuit. For the purpose of obtaining the spectrum and making an internal-impedance (resistance) measurement,  $R_L$  may have values from 6 to 100 K without appreciably altering the spectrum.<sup>2</sup>

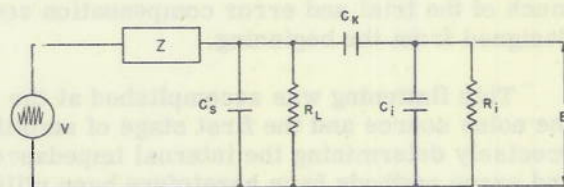
With the foregoing assumptions in mind, it is possible to reduce the circuit of Figure 4A to that of Figure 4B; and at the same time  $Z$  (assumed to be purely resistive) can be determined by adjusting  $R$  (Figure 4B) until the voltage is one-half its value on open circuit. Appendix I explains this in more detail. Measurement of  $R$  with an ohmmeter is sufficiently accurate, and, for purposes here, this measured value is the internal impedance.

<sup>2</sup> Cobine, J. D. and Curry, J. R. "The Characteristics of the Sylvania 6D4 Miniature Gas Triode as a Noise Source for the Range 0.1-5 Mc" NDRC, Division (15) RRL 411-169, Appendix Graphs H200-A71 and H200-A72, (Unclassified), March 30, 1945



$Z$  = INTERNAL IMPEDANCE OF GENERATOR  
 $V$  = INTERNAL VOLTAGE  
 $C'_S$  = SOCKET CAPACITY & TUBE CAPACITY  
 $R_L$  = PLATE-LOAD RESISTOR  
 $C_K$  = COUPLING CAPACITOR  
 $E$  = TERMINAL VOLTAGE

Figure 2 - Equivalent circuit of 6D4 as noise generator



$Z$  = INTERNAL IMPEDANCE OF GENERATOR  
 $C'_S$  = SOCKET CAPACITY & TUBE CAPACITY  
 $R_L$  = PLATE-LOAD RESISTOR  
 $C_K$  = COUPLING CAPACITOR  
 $C_i$  = INPUT CAPACITY OF NOISE ANALYZER  
 $R_i$  = GRID RESISTANCE OF NOISE ANALYZER  
 $V$  = INTERNAL VOLTAGE

Figure 3 - Equivalent circuit of noise generator when connected to the noise analyzer



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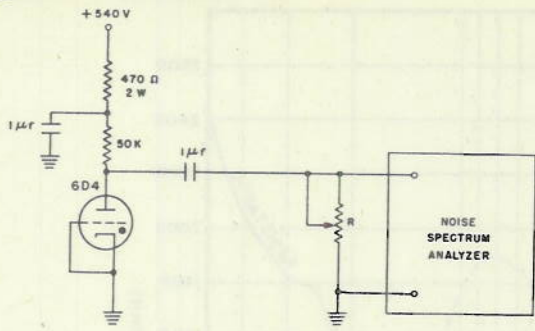


Figure 4A - Setup for measuring internal impedance

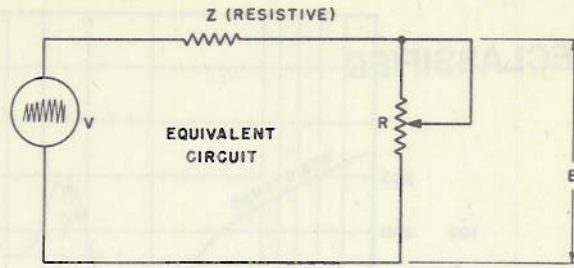


Figure 4B - Equivalent circuit of method for measuring internal impedance of noise generator

Figures 5 and 6 are graphs of the two typical noise spectra obtainable from 6D4's and their accompanying impedance characteristics as measured by the method already outlined. There appear to be at least two types of 6D4's, since two different noise spectra are present, one with a peak at 650 kc, the other with a slightly different shape and a peak at 800 kc.<sup>3</sup> When several tubes were broken open for inspection to ascertain any constructional differences, the position of the grid slot was found to vary with respect to the crimp in the plate, either facing the crimp or the opposite side. Just how these dissimilarities in construction affected the noise spectrum was debatable, since some of each type showed like spectra.

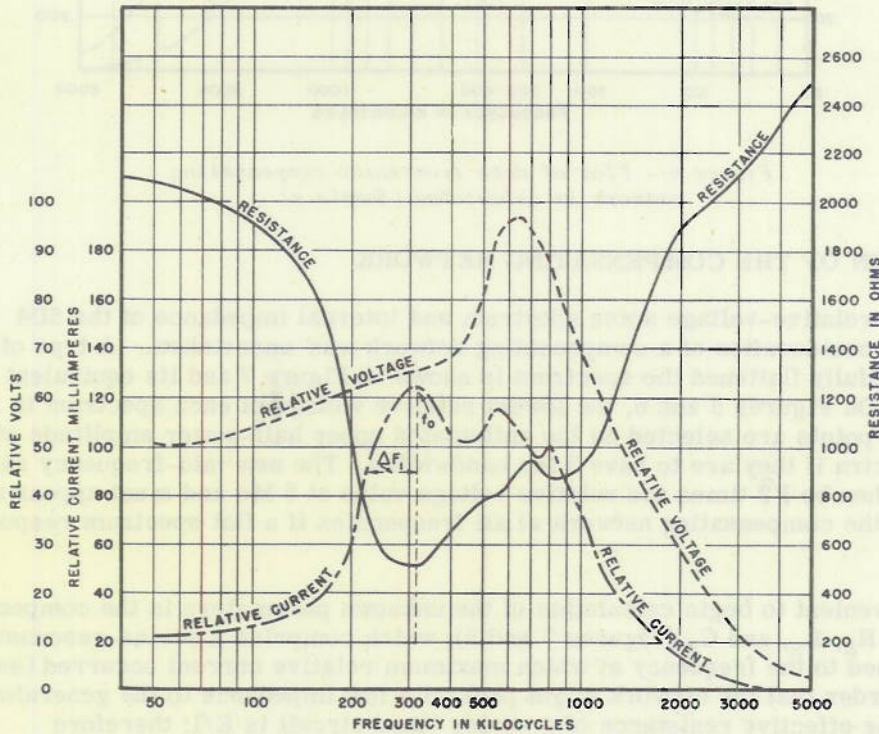


Figure 5 - Plot of data from which compensating network is calculated (Sample 1)

<sup>3</sup> Ibid. Graph # 11200-ATE

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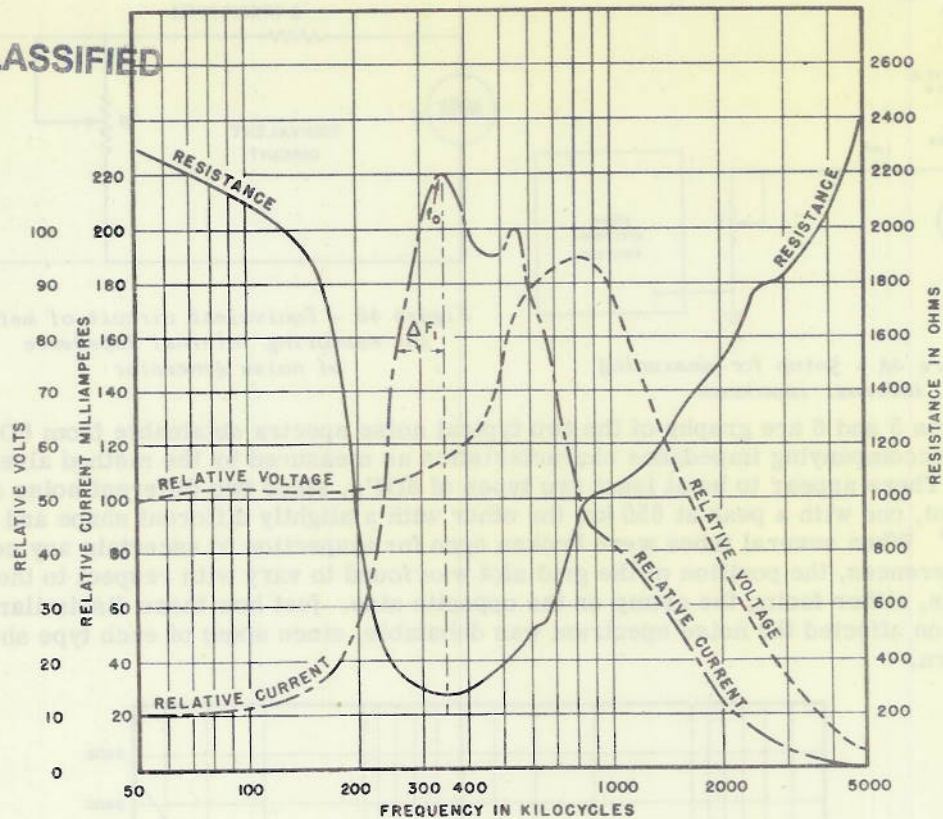


Figure 6 - Plot of data from which compensating network is calculated (Sample 2)

#### CALCULATION OF THE COMPENSATING NETWORK

Once the relative-voltage noise spectrum and internal impedance of the 6D4 had been determined, consideration of a compensating network was undertaken. A type of network which successfully flattened the spectrum is shown in Figure 7 and its equivalent circuit in Figure 8. On Figures 5 and 6, the lowest relative voltage of each spectrum is 3 to 4 volts. These points are selected as the anticipated upper half-power amplitude of the compensated spectra if they are to have 5 Mc bandwidths. The new mid-frequency response voltage will then be  $\sqrt{2}$  times the relative voltage value at 5 Mc and must appear across the output of the compensating network at all frequencies if a flat spectrum response is expected.

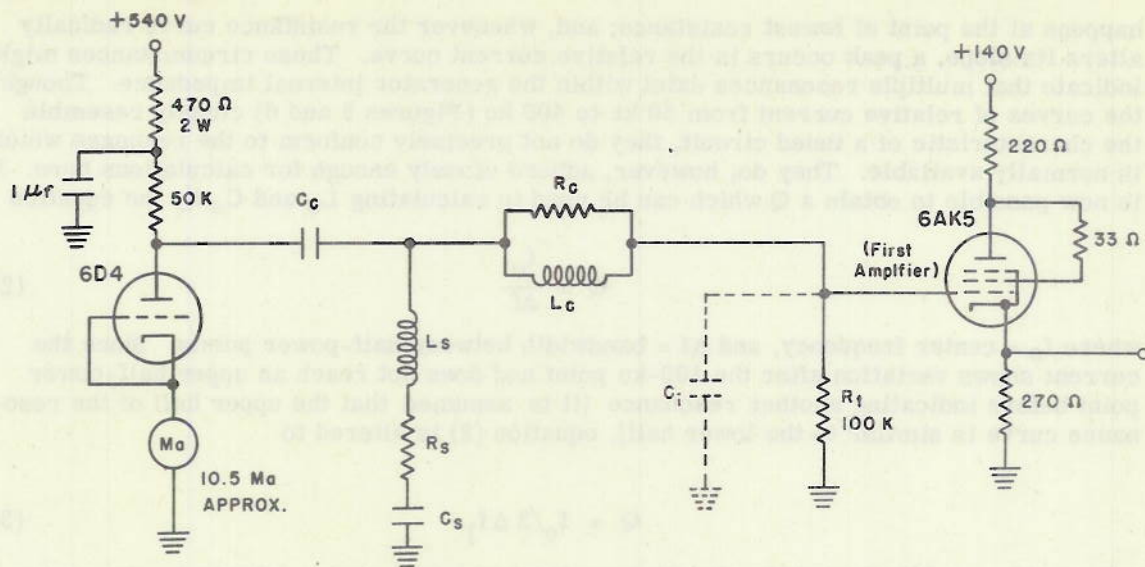
It is convenient to begin calculation of the unknown parameters in the compensating network with  $R_s$ ,  $L_s$ , and  $C_s$  (Figures 7 and 8), which comprise a series-resonant circuit purposely tuned to the frequency at which maximum relative current occurred (see Figures 5 and 6), in order that the network might present a low impedance to the generator. At resonance, the effective resistance of a series tuned circuit is  $E/I$ ; therefore

$$R_s = \frac{\sqrt{2} \text{ times the relative voltage at 5 Mc}}{I}, \quad (1)$$

where  $I$  is the maximum current. On Figures 5 and 6 also, the maximum relative current

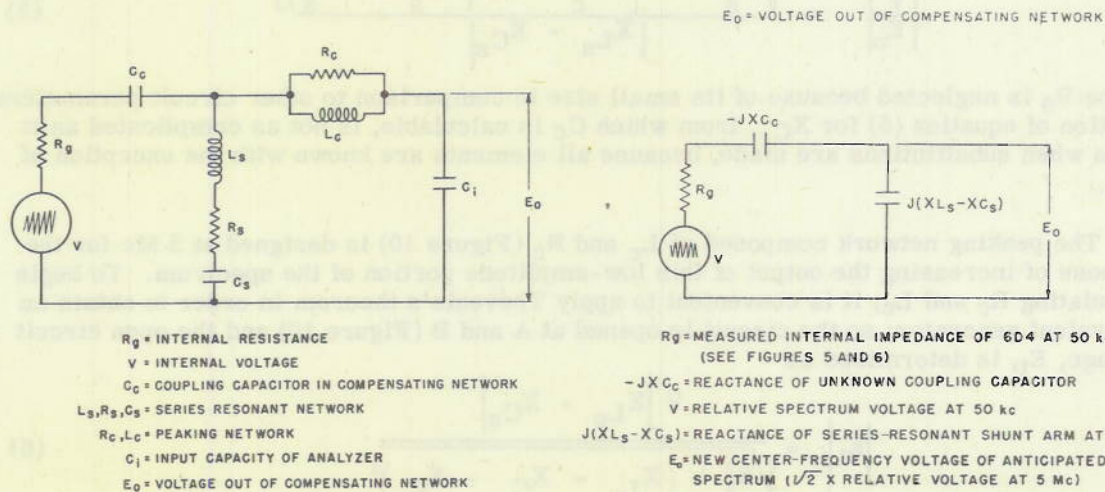
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$C_c$  = COUPLING CAPACITOR IN COMPENSATING NETWORK  
 $L_s, C_s, R_s$  = SERIES-RESONANT NETWORK  
 $R_c, L_c$  = PEAKING NETWORK  
 $C_i$  = INPUT CAPACITY OF AMPLIFIER  
 $R_t$  = GRID RESISTOR

Figure 7 - Type of network which flattened the noise spectrum



$R_g$  = INTERNAL RESISTANCE  
 $V$  = INTERNAL VOLTAGE  
 $C_c$  = COUPLING CAPACITOR IN COMPENSATING NETWORK  
 $L_s, R_s, C_s$  = SERIES RESONANT NETWORK  
 $R_c, L_c$  = PEAKING NETWORK  
 $C_i$  = INPUT CAPACITY OF ANALYZER  
 $E_0$  = VOLTAGE OUT OF COMPENSATING NETWORK

$R_g$  = MEASURED INTERNAL IMPEDANCE OF 6D4 AT 50 kc  
 (SEE FIGURES 5 AND 6)  
 $-JXC_c$  = REACTANCE OF UNKNOWN COUPLING CAPACITOR  
 $V$  = RELATIVE SPECTRUM VOLTAGE AT 50 kc  
 $J(XL_s - XC_c)$  = REACTANCE OF SERIES-RESONANT SHUNT ARM AT 50 kc  
 $E_0$  = NEW CENTER-FREQUENCY VOLTAGE OF ANTICIPATED SPECTRUM ( $1/\sqrt{2}$  X RELATIVE VOLTAGE AT 5 Mc)

Figure 8 - Equivalent circuit of noise generator and compensating network

Figure 9 - 50-kc equivalent circuit of compensating network

happens at the point of lowest resistance; and, whenever the resistance curve radically alters its slope, a peak occurs in the relative current curve. These circumstances might indicate that multiple resonances exist within the generator internal impedance. Though the curves of relative current from 50 kc to 400 kc (Figures 5 and 6) closely resemble the characteristic of a tuned circuit, they do not precisely conform to the response which is normally available. They do, however, adhere closely enough for calculations here. It is now possible to obtain a  $Q$  which can be used in calculating  $L_s$  and  $C_s$  by the equation

$$Q = \frac{f_0}{\Delta f} \quad (2)$$

where  $f_0$  = center frequency, and  $\Delta f$  = bandwidth between half-power points. Since the current shows variation after the 400-kc point and does not reach an upper half-power point before indicating another resonance (it is assumed that the upper half of the resonance curve is similar to the lower half), equation (2) is altered to

$$Q = f_0 / 2 \Delta f_1 \quad (3)$$

where  $\Delta f_1 = \Delta f / 2$ , the half bandwidth from the lower half-power point to  $f_0$ , the center frequency. With this  $Q$ ,  $C_s$  and  $L_s$  are determinable from

$$Q = \frac{1}{R_s \omega C_s} = \frac{\omega L_s}{R_s} \quad (4)$$

Next, the value of  $C_c$  (Figures 7 and 8) must be calculated at the lowest frequency of the spectrum to be passed by the compensating network; in this case a 50-kc equivalent circuit as in Figure 9 is applicable. To obtain  $X_{C_c}$ ,

$$\left| \frac{V}{E_0} \right| = \frac{\sqrt{R_g^2 + [X_{C_c} + (X_{C_s} - X_{L_s})]^2}}{|X_{L_s} - X_{C_s}|} \quad (5)$$

where  $R_s$  is neglected because of its small size in comparison to other circuit parameters. Solution of equation (5) for  $X_{C_c}$ , from which  $C_c$  is calculable, is not as complicated as it looks when substitutions are made, because all elements are known with the exception of  $X_{C_c}$ .

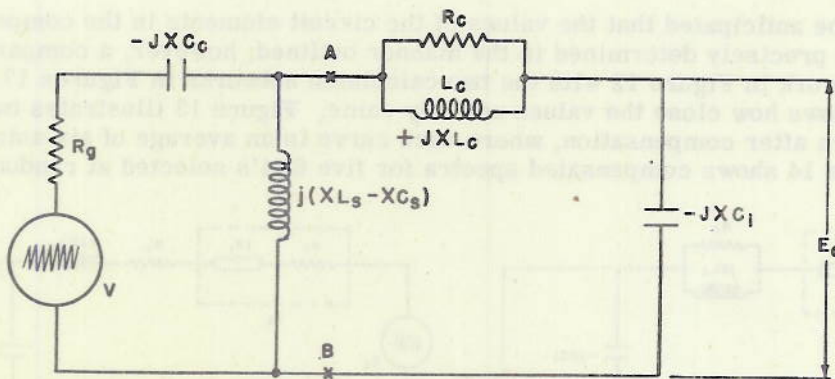
The peaking network composed of  $L_c$  and  $R_c$  (Figure 10) is designed at 5 Mc for the purpose of increasing the output of this low-amplitude portion of the spectrum. To begin calculating  $R_c$  and  $L_c$ , it is convenient to apply Thévenin's theorem in order to obtain an equivalent generator; so the circuit is opened at A and B (Figure 10) and the open circuit voltage,  $E_t$ , is determined as

$$\left| E_t \right| = \frac{V |X_{L_s} - X_{C_s}|}{\sqrt{R_g^2 + (X_{L_s} - X_{C_s} - X_{C_c})^2}} \quad (6)$$

The next step is to short out the sources of emf and determine the Thévenin impedance looking back into the network from terminals A and B (Figure 10). Then

$$Z_t = \frac{(R_g - jX_{C_c}) \left[ j(X_{L_s} - X_{C_s}) \right]}{R_g + j(X_{L_s} - X_{C_s} - X_{C_c})} \quad (7)$$

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- $R_g$  = MEASURED INTERNAL IMPEDANCE OF 6D4 AT 5 Mc
- $V$  = RELATIVE SPECTRUM VOLTAGE AT 5 Mc
- $-jX_{C_c}$  = REACTANCE OF COUPLING CAPACITOR AT 5 Mc
- $j(X_{L_s} - X_{C_s})$  = REACTANCE OF SERIES-RESONANT SHUNT ARM AT 5 Mc
- $R_c, jX_{L_c}$  = UNKNOWN PARAMETERS OF 5-Mc PEAKING NETWORK
- $-jX_{C_i}$  = INPUT CAPACITIVE REACTANCE OF FIRST STAGE OF AMPLIFICATION
- $E_o$  = NEW CENTER-FREQUENCY VOLTAGE OF ANTICIPATED SPECTRUM ( $1/\sqrt{2}$  X RELATIVE VOLTAGE AT 5 Mc)

Figure 10 - 5-Mc equivalent circuit of compensating network

The equivalent network resulting from the application of Thévenin's theorem is shown on Figure 11A. In order that  $R_c$  and  $L_c$  be calculated, it is feasible to change the equivalent circuit further by making use of an equivalent series combination of  $R_c$  and  $X_{L_c}$  designated on Figure 11B by  $R'_c$  and  $X'_{L_c}$ . Now  $X_t$ , the reactive part of  $Z_t$ , plus  $X'_{L_c}$  is designed to resonate with  $X_{C_i}$  at 5 Mc, and since  $X_t$  is known,

$$X'_{L_c} = X_{C_i} - X_t \quad (8)$$

Because resonance exists,  $j(X_t + X'_{L_c} - X_{C_i}) = 0$ , and  $R'_c$  may be found by solving

$$\left| \frac{E_o}{E_t} \right| = \frac{|X_{C_i}|}{R'_c + R_t} \quad (9)$$

Enough information is now available so that  $R'_c$  and  $X'_{L_c}$  may be determined, but they must be converted to the original parallel combination for practical application; hence,

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$$R_c = \frac{(R'_c)^2 + (X'_Lc)^2}{R'_c} \tag{10}$$

and

$$X_{Lc} = \frac{(R'_c)^2 + (X'_Lc)^2}{X'_Lc} \tag{11}$$

It could not be anticipated that the values of the circuit elements in the compensating network could be precisely determined in the manner outlined; however, a comparison of the practical network in Figure 12 with the two calculated networks in Figures 17 and 18 of Appendix II shows how close the values actually came. Figure 13 illustrates two possibly obtainable spectra after compensation, where each curve is an average of six noise generators; and Figure 14 shows compensated spectra for five 6D4's selected at random.

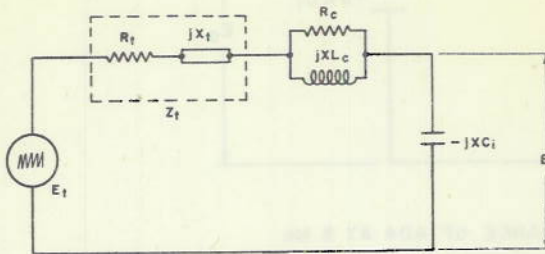


Figure 11A - Thevenin equivalent circuit of 5-μc network

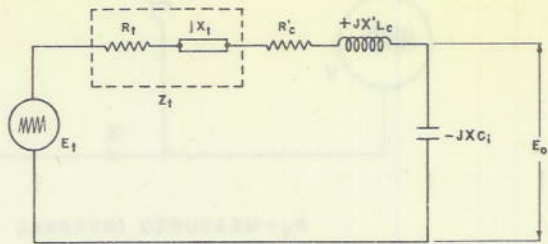


Figure 11B - Thevenin equivalent circuit of 5-μc network with series transformation

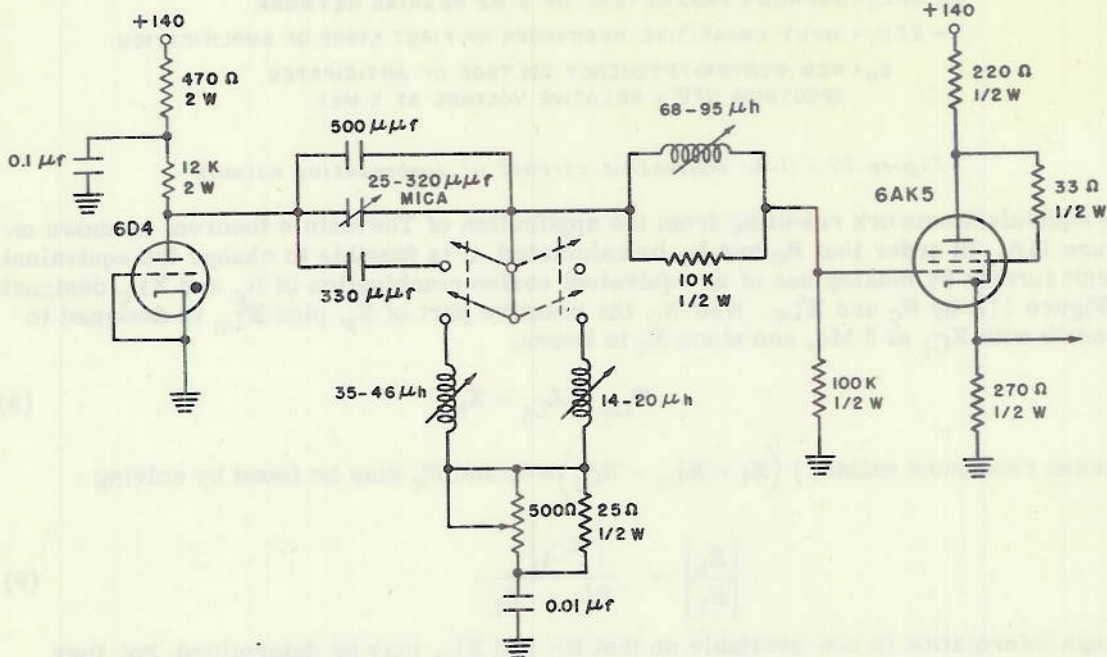


Figure 12 - Practical compensating network

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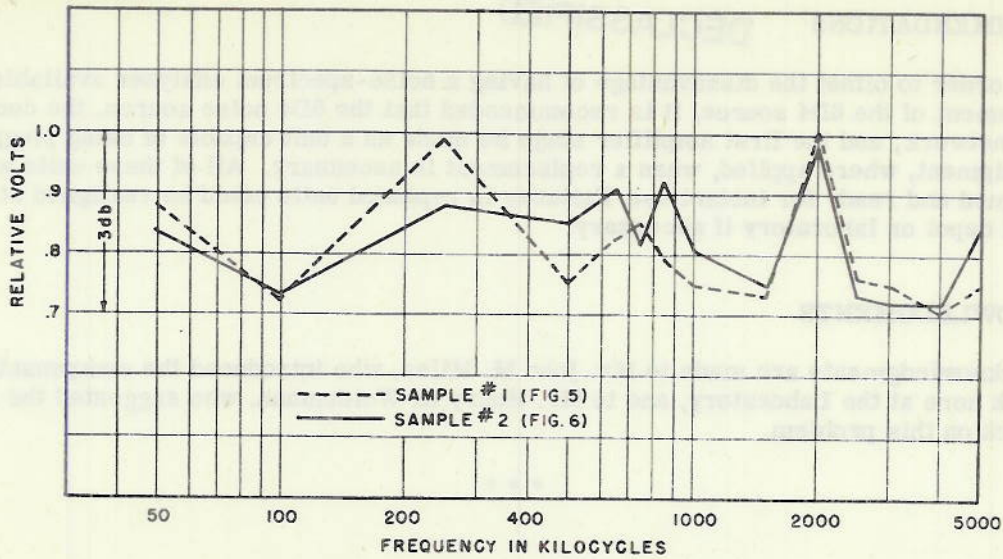


Figure 13 - Typical spectra after compensation

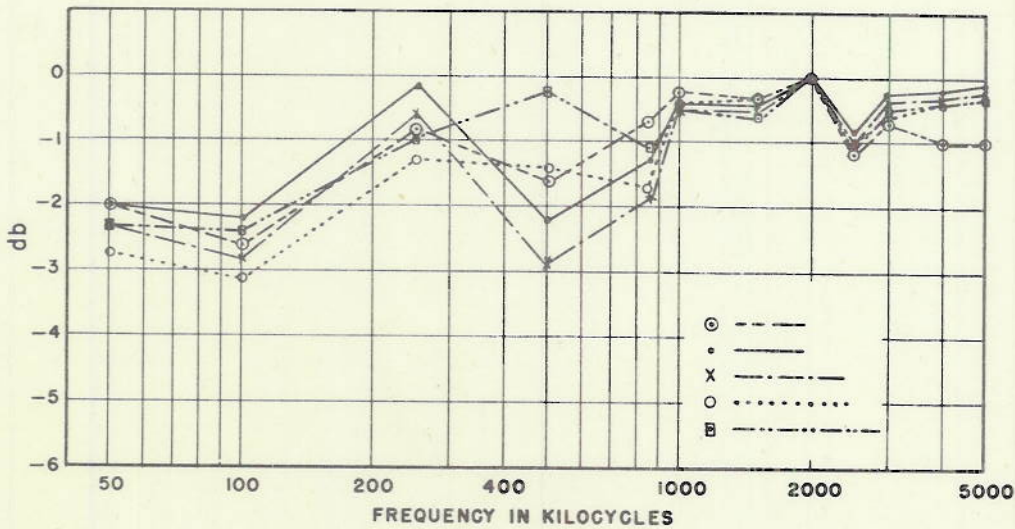


Figure 14 - Typical spectra after compensation

CONCLUSIONS

With the network discussed in this report and its method of determination, it is possible to eliminate much of the tedious trial and error compensation of amplifiers into which the noise spectrum of the 6D4 is fed. Though the spectrum level is attenuated some 35 db there is still a usable noise output somewhat higher in amplitude than that of the 931-A photomultiplier noise source and an entire amplifier stage could possibly be eliminated. The main disadvantage is the necessity of having a noise-spectrum analyzer available when installing a new 6D4 source, since there are differences apparent from tube to tube which could require readjustment of the compensating network.

RECOMMENDATIONS

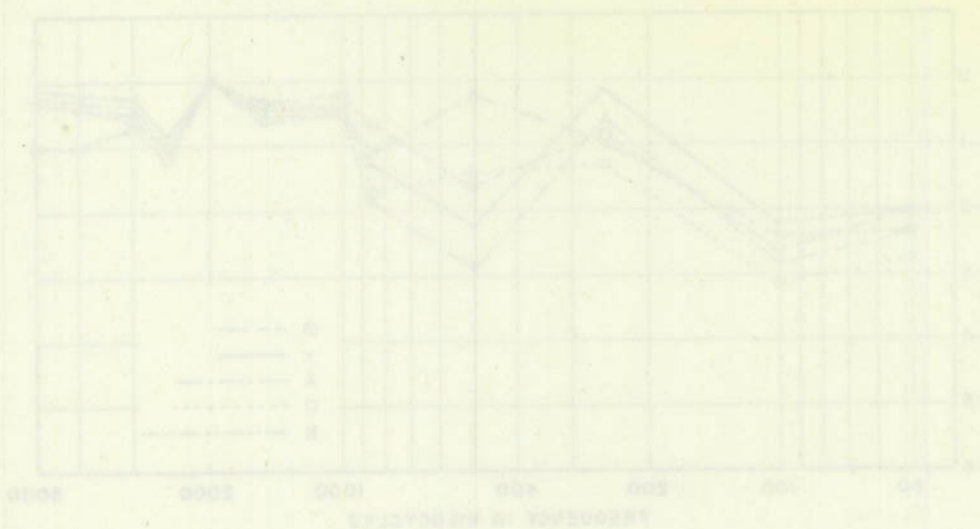
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In order to offset the disadvantage of having a noise-spectrum analyzer available upon replacement of the 6D4 source, it is recommended that the 6D4 noise source, the compensating network, and the first amplifier stage be made as a unit capable of being plugged into the equipment, where applied, when a replacement is necessary. All of these units would be prealigned and ready for instant use. Failures in replaced units could be realigned at some central depot or laboratory if necessary.

ACKNOWLEDGMENTS

Acknowledgments are made to Mr. John M. Miles, who introduced the compensating network here at the Laboratory, and to Mr. Henry K. Weidemann, who suggested the method of attack on this problem.

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APPENDIX I  
 Explanation of the Method Used to Measure the Internal Impedance  
 of the 6D4 as a Noise Source

In Figures 15 and 16

- $E_o$  = Open circuit voltage
- $E_g$  = Generator internal voltage
- $R_g$  = Generator internal resistance
- $R$  = (Externally connected) load resistance
- $E_r$  = Voltage across R.

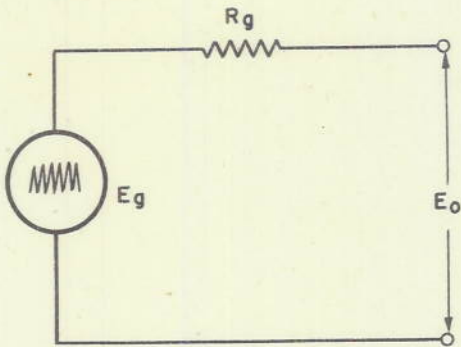


Figure 15 - Generator on open circuit

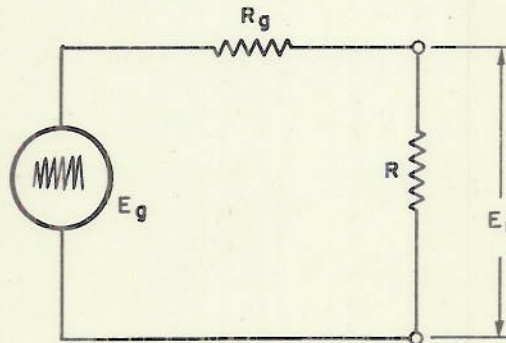


Figure 16 - Generator under load

It is apparent that

$$E_r = \frac{E_g R}{R_g + R}$$

On open circuit,  $E_g = E_o$ . Therefore,

$$E_r = \frac{E_o R}{R_g + R}$$

or

$$\frac{E_r}{E_o} = \frac{R}{R_g + R}$$

If  $E_r/E_0 = 1/2$ , then

$$\frac{1}{2} = \frac{R}{R_g + R}$$

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$$R_g + R = 2R$$

$$R_g = R.$$

Hence, the internal resistance is equal to the external resistance.

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**APPENDIX II**  
**Sample Calculations Involving Methods Already Discussed,**  
**With a Comparison of Calculated Values of Network Parameters**  
**and the Practical Compensating Network**

Using Figure 5 as the criterion of a typical noise spectrum and internal resistance measurement, equations 1 and 3 through 11 are applied as follows:

$$(1) \quad R_s = \frac{\sqrt{2} \text{ times relative voltage at 5 Mc}}{I}$$

where the relative voltage is 3 taken from the relative voltage curve on Figure 5; and the maximum current,  $I$ , is 0.126 ampere taken from the curve of relative current; so

$$\begin{aligned} R_s &= \frac{\sqrt{2} \text{ times } 3}{0.126} \\ &= 33.7 \text{ ohms.} \end{aligned}$$

$$(3)* \quad Q = \frac{f_0}{2 \Delta f_1}$$

For this particular case  $f_0 = 315$  kc, taken from the relative current curve at its maximum amplitude.  $f_1 = 90$  kc, read on the same curve of relative current; therefore

$$\begin{aligned} Q &= \frac{315}{2 \text{ times } 90} \\ &= 1.75. \end{aligned}$$

$$(4) \quad Q = \frac{1}{\omega R_s C_s} = \frac{\omega L_s}{R_s}$$

By substituting into (4) values calculated in equations (1) and (3),  $C_s$  and  $L_s$  may be computed.

$$\begin{aligned} \omega L_s &= 1.75 \text{ times } 33.7 \\ &= 59 \text{ ohms at } 315 \text{ kc.} \end{aligned}$$

Because resonance exists,  $X_{L_s} = X_{C_s}$ ; therefore,  $C_s = 0.0086$  microfarad and  $L_s = 29.7$  microhenries.

\* Equation (2) is not used here.

In order to continue calculations and apply equation (5),  $X_{L_S}$  and  $X_{C_S}$  must be converted to their 50 kc values.  $X_{C_S}$  at 50 kc = 372 ohms and  $X_{L_S}$  at 50 kc = 9.4 ohms.

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$$\left| \frac{V}{E_0} \right| = \frac{\sqrt{R_g^2 + [X_{C_c} + (X_{C_S} - X_{L_S})]^2}}{|X_{L_S} - X_{C_S}|}$$

Substituting the 50 kc value of  $R_g$  as taken from the curve of resistance (Figure 5) and the 50 kc values of  $X_{C_S}$  and  $X_{L_S}$ , a solution of equation (5) for  $X_{C_c}$  is now possible, where  $V$  is the 50 kc relative voltage value and  $E_0 = \sqrt{2}$  times 3.

$$\frac{51}{4.2} = \frac{\sqrt{(2100)^2 + (X_{C_c} + 363)^2}}{363},$$

$$X_{C_c} = 3,522 \text{ ohms, so}$$

$$C_c = 910 \text{ micromicrofarads.}$$

$$(6) \quad |E_t| = \frac{V |X_{L_S} - X_{C_S}|}{\sqrt{R_g^2 + (X_{L_S} - X_{C_S} - X_{C_c})^2}}$$

From Figures 5 and 10,  $R_g = 2500$  ohms at 5 Mc,  $V = 3$  volts relative,  $X_{L_S}$ ,  $X_{C_S}$ , and  $X_{C_c}$  are reactance values determined at 5 Mc.

$$E_t = \frac{3(936)}{\sqrt{(2500)^2 + (901)^2}}$$

$$= 1.06 \text{ volts.}$$

$$(7) \quad Z_t = \frac{(R_g - jX_{C_c}) [j(X_{L_S} - X_{C_S})]}{R_g + j(X_{L_S} - X_{C_S} - X_{C_c})}$$

The numerical values substituted in (7) are the same as in (6), where  $X_{C_c} = 35.2$  ohms at 5 Mc.

$$Z_t = \frac{(2500 - j35.2) (j936)}{2500 + j901}$$

$$= 310 + j824 \text{ vector ohms.}$$

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$$(8) \quad X'_{L_c} = X_{C_i} - X_t$$

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$X'_{L_c}$  is the series equivalent of the peaking inductance,  $X_{L_c}$ , (shown on Figure 11B),

$X_{C_i} = 3,183$  ohms (assumed input capacity of amplifier at 5 Mc is 10 micromicrofarads),

$X_t = 824$  ohms from (7), and

$$\begin{aligned} X'_{L_c} &= 3,183 - 824 \\ &= 2,359 \text{ ohms.} \end{aligned}$$

$$(9) \quad \frac{E_o}{E_t} = \frac{X_{C_i}}{R'_c + R_t},$$

$$\frac{4.2}{1.06} = \frac{3,183}{R'_c + 310},$$

$$R'_c = 494 \text{ ohms.}$$

Now it remains to convert  $R'_c$  and  $X'_{L_c}$  to their parallel equivalents.

$$(10) \quad R_c = \frac{(R'_c)^2 + (X'_{L_c})^2}{R'_c},$$

$$R_c = \frac{(494)^2 + (2359)^2}{494}$$

$$= 10,562 \text{ ohms.}$$

$$(11) \quad X_{L_c} = \frac{(R'_c)^2 + (X'_{L_c})^2}{X'_{L_c}},$$

$$X_{L_c} = \frac{(494)^2 + (2359)^2}{2359}$$

$$= 2,462 \text{ ohms,}$$

$$L_c = 78.4 \text{ microhenries.}$$

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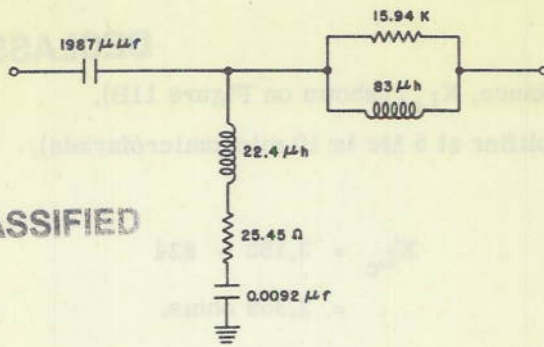


Figure 17 - Sample 1

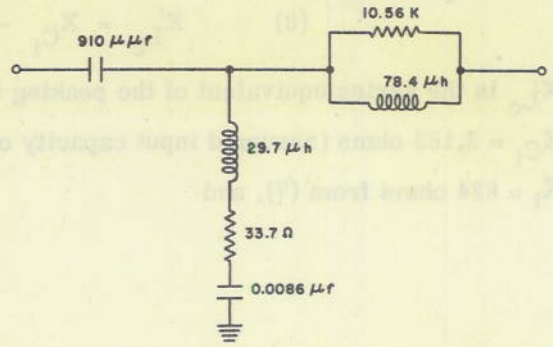


Figure 18 - Sample 2

Calculated compensating networks

Figure 17 shows the calculated compensating network with the values just determined in this appendix. In a similar manner the values of the parameters of Figure 18 were calculated using data obtained from Figure 6.

\* \* \*

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## LIST OF SYMBOLS USED IN CALCULATIONS

$R_L$	6D4 plate load resistor
$C_k$	Coupling capacitor
$V$	Internal voltage of noise generator
$Z$	Internal impedance of noise generator
$C'_S$	6D4 socket capacity plus tube capacity
$E$	Terminal voltage
$C_i$	Input capacity of noise analyzer or first amplifier
$R_i$	Grid resistance of noise analyzer
$R$	Resistor used for loading noise generator
$C_c$	Coupling condenser in compensating network
$\left. \begin{matrix} L_s \\ R_s \\ C_s \end{matrix} \right\}$	Series resonant shunt arm of compensating network
$\left. \begin{matrix} R_c \\ L_c \end{matrix} \right\}$	Elements of peaking network
$R_T$	Grid resistor of first amplifier
$R_g$	Assumed internal resistance of noise generator
$E_o$	Voltage out of compensating network (new center frequency voltage)
$-jX_{C_c}$	Reactance of compensating network coupling capacitor at 50 kc
$-j(X_{C_s} - X_{L_s})$	Reactance of series resonant shunt arm
$jX_{L_c}$	Reactance of peaking inductance
$E_t$	Thévenin equivalent generator
$Z_t$	Thévenin equivalent internal impedance
$R_t$	Resistance component of Thévenin impedance

$jX_{L_t}$	Reactive component of Thévenin impedance
$R'_c$	Series equivalent of $R_c$
$jX'_{L_c}$	Series equivalent of $jX_{L_c}$
$f_o$	Center frequency
$\Delta f$	Bandwidth between half-power points
$\Delta f_1$	$\frac{1}{2}$ the bandwidth between half-power points

\* \* \*

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